# Cosmic Rays and the Search for a Violation of Lorentz Invariance

### l. Cosmic rays

Phenomenology, GZK cutoff

#### **II. Violation of Lorentz Invariance**

Theory, maximal attainable velocities Applications to decays, Čerenkov radiation GZK cutoff and neutrino oscillation

### III. Cosmic $\gamma$ -rays

Radiation of blazars and  $\gamma$ -Ray-Bursts (Photons in a non-commutative space)

IV. **Summary and Appendix** News from Pierre Auger Obs.

# I. Cosmic Rays

High energy particles and nuclei of cosmic origin

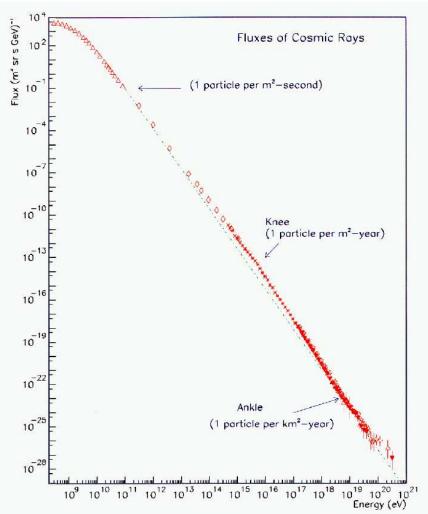
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1912 Discovery by V.F. Hess with an electroscope on a balloon : ionising radiation decreases up to 2000 m (radioactivity from earth) but rises again above [Hess: \rightarrow 5350 m; W. Kolhörster (1913/4) \rightarrow 6300 m] \Rightarrow Cosmic origin (beyond sun)
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1938 P. Auger: separated Geiger counters detect correlated events. Extended Air Shower

Cascade triggered by a high energy primary particle. Estimate:  $E \ge 10^{15} \text{ eV}$ 

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Knowledge today: \mathbf{E} \approx \mathbf{10}^9 \dots \mathbf{10}^{20} \ eV at high energy: \approx 90 % protons, 9 % \alpha, plus a few heavier nuclei; or Fe ions (?)
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Isotropic; for charged rays source cannot be located (traditional picture) [ deflection by interstellar magnetic fields  $\sim O(\mu \text{G})$  ]



Flux of cosmic rays vs. energy, over broad interval essentially  $\propto E^{-3}$ 

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Origin ??? Historic proposal: Fermi mechanisms Collisions in a magnetic cloud. Later version : shock waves in gas of a supernova. Explanation at best up to \sim 10^{14}~{\rm eV}. Predicts energy density \propto E^{-2} [ Observations close to E^{-3} ]
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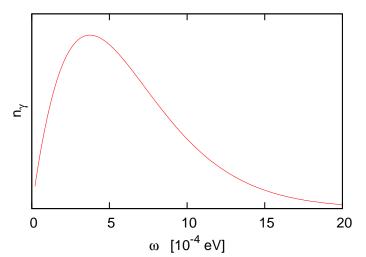
### Two classes of scenarios:

- "Top-down": Decay of extremely heavy particles generated in Big Bang  $\rightarrow$  energy available (magnetic monopoles, "wimpzillas" . . . ??  $\rightarrow$  high-E  $\gamma$ ,  $\nu$  flux, not observed)

## 1965 A. Penzias/R. Wilson discover Cosmic Microwave Background

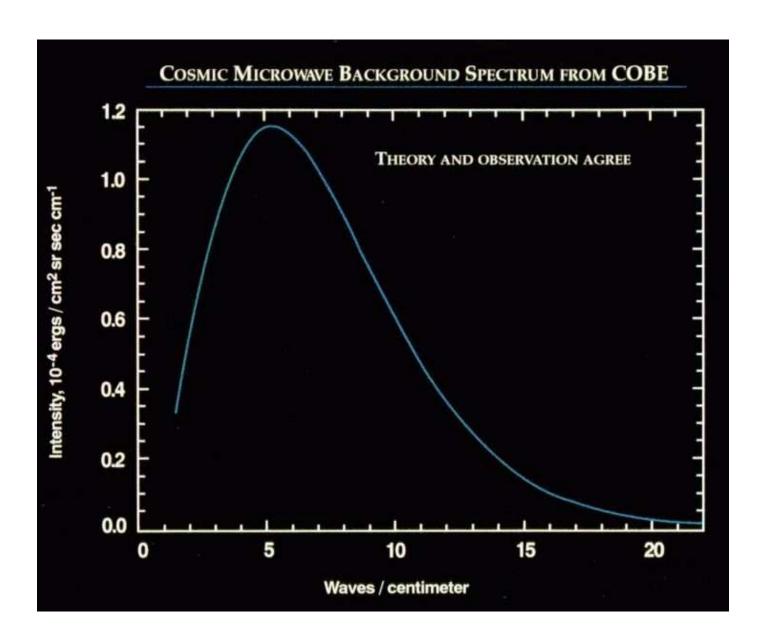
Relic of the Big Bang, photons decoupled after  $pprox 3.8 \cdot 10^5$  years

Very precise Planck distribution :  $dn_\gamma/d\omega \propto \frac{\omega^2}{e^{\omega/kT}-1}$  ,  $~\omega$  :  $\gamma$ -energy



$$\mathbf{T}=\mathbf{2.725}(\mathbf{1})\ \mathsf{K}$$
  $\int_0^\infty d\omega\, n_\gamma{}'(\omega) \simeq 411\ \mathrm{cm}^{-3}$ 

$$\langle \omega 
angle = \mathbf{6} \cdot \mathbf{10}^{-4} \; \mathbf{eV} \; ,$$
  $\langle \lambda 
angle \simeq 1.9 \; \mathsf{mm} \; \; (\mathsf{microwaves})$ 



# **GZK** Cutoff

1966 K. Greisen (Cornell), G.T. Zatsepin und V.A. Kuz'min (Lebedev)

Prediction: Cosmic rays have "cutoff" at  $E \approx 6 \cdot 10^{19} \text{ eV}$ 

Reason: Photopion production, in particular:

$$p + \gamma \rightarrow \Delta(1232 \text{ MeV}) \stackrel{\rightarrow}{\rightarrow} p + \pi^0$$
  
 $\rightarrow n + \pi^+, n \rightarrow p + e^- + \bar{\nu}_e$   $\left.\right\} 99.4\%$ 

[ Further resonances: 
$$\Delta(1620,\ 1700,\ \dots)$$
 ,  $p^*(1440,\ 1520\ \dots)$  etc.  $\to$   $p+\pi$  or  $p+2\pi$  ]

Threshold for proton energy:  $E_p = E_0$  (c = 1)

$$s = (E_0 + \omega)^2 - (\vec{p}_p + \vec{p}_{\gamma})^2 \qquad ("laboratory", FRW metrics)$$

$$= \underbrace{E_0^2 - \vec{p}_p^2}_{m_p^2} + 2E_0 \omega - 2\vec{p}_p \, \vec{p}_{\gamma} \simeq m_p^2 + \underbrace{4E_0 \omega}_{\text{head-on}} \stackrel{!}{=} m_{\Delta}^2 \qquad (\text{rest frame of } \Delta)$$

$$E_0 = \frac{m_{\Delta}^2 - m_p^2}{4\omega} \stackrel{\text{e.g. } \omega = 5\langle \omega \rangle}{=} \underbrace{6 \cdot 10^{19} \text{ eV}}$$

Further kinemat. transformations o Inelasticity  $K:=rac{\Delta E_p}{E_p}=rac{1}{2}\left[1-rac{m_p^2-m_\pi^2}{s}
ight]$ 

Rest frame of the proton:  $s=(m_p+\bar{\omega})^2-\vec{p}_{\gamma}^{\,2}=m_p^2+2m_p\,\bar{\omega}$ 

Doppler effect:  $\bar{\omega} = \gamma \omega (1 - v_p \cos \theta)$  ( $\theta$ : scattering angle in "laboratory")  $\gamma = \frac{E_p}{m_p}$ , e.g.  $\frac{E_0}{m_p} \sim 10^{11} \Rightarrow \langle \bar{\omega} \rangle_{\theta} \simeq 180~{\rm MeV} \cdot \frac{E_p}{E_0}$ 

$$K(\langle \bar{\omega} \rangle) = \frac{1}{2} \left[ 1 - \frac{m_p^2 - m_\pi^2}{m_p(m_p + 2\langle \bar{\omega} \rangle)} \right] = \begin{cases} 0.15 & \langle \bar{\omega} \rangle = 180 \text{ MeV} \\ 0.20 & \langle \bar{\omega} \rangle = 300 \text{ MeV}, E_p = 2E_0 \end{cases}$$

au : decay time of energy  $E_p > E_0$  during journey through the Universe

$$\frac{1}{\tau(E_p)} = -\frac{kT}{2\pi^2 \gamma^2} \int_{\bar{\omega}_0}^{\infty} d\bar{\omega} \, \sigma(\bar{\omega}) K(\bar{\omega}) \, \underline{\bar{\omega}} \ln \left[ 1 - e^{-\bar{\omega}/(2\gamma kT)} \right]$$
from Planck distribution

(F.W. Stecker, '68)

Cross-section  $\sigma$  is known from experiments: proton at rest in  $\gamma$  radiation  $\sigma \approx 0.1 \text{ mb}$  (e.g. K.K. Wilson, '58)

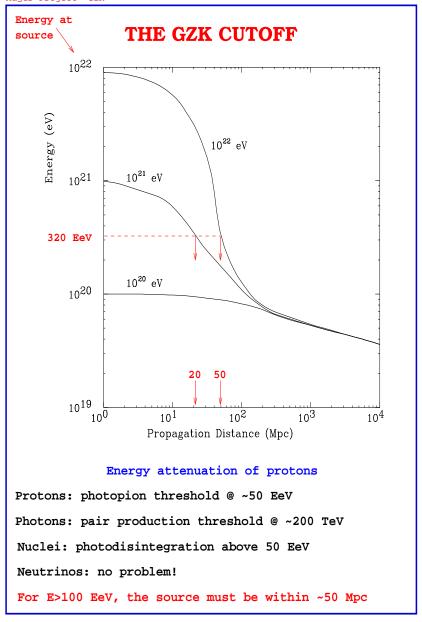
 $\Rightarrow$  Computation of au and corresp. path length  $\ell \simeq au c \sim 10\dots 20~{
m Mpc}$ 

Minor corrections (additional photopion productions channels, discrete process . . . )

Heavy nuclei: photodisintegration  $\rightarrow$  attenuation length even shorter

Also for protons: very high starting energy  $\rightarrow$  energy loss more rapid

 $\Rightarrow$  Range with E > GZK cutoff is maximally  $\sim 50 \dots 100 \; \mathrm{Mpc}$ 



 $[R_{
m galactic\ plane} \sim 15\ {
m kpc}] \ll$  attenuation length  $\ll [R_{
m visible\ Universe} \sim 14\ {
m Gpc}]$ Source should be near-by (e.g. Virgo galaxy cluster, 20 Mpc).

Homogeneously distributed sources  $\to$  pile-up at  $E \lesssim E_0$  (5 ·  $10^{17}~{\rm eV} < E < E_0~:~p+\gamma \to p+e^++e^-$  but  $\Delta E$  is small).

No sufficient acceleration mechanism is known, in particular not in our vicinity

→ Exceeding the GZK cutoff would be mysterious

#### **Observations**

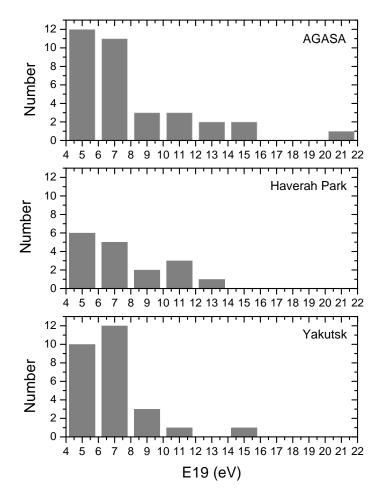
- 1963 J. Linsley et al. (New Mexico) one event at  $10^{20}~{\rm eV}$
- 1971 K. Suga et al. (Tokyo) new super-GZK event
- 1991 Fly's Eye (Utah) claims world record:  $3 \cdot 10^{20} \, \mathrm{eV} = 48 \, \mathrm{J} = E_{\mathrm{kin}}^{\mathrm{tennis} \, \mathrm{ball}} (147 \, \mathrm{km/h})$

 $21^{\mathrm{st}}$  century : AGASA (Japan) numerous super-GZK events.

Spectrum agrees with Yakutsk (Russia) and Haverah Park (England),

but in contradiction to HiRes (Utah): seems to confirm cutoff.

De Marco/Blasi/Olinto (2003): Discrepancy might be explained statistically.



Super-GZK events at AGASA, Haverah Park and Yakutsk

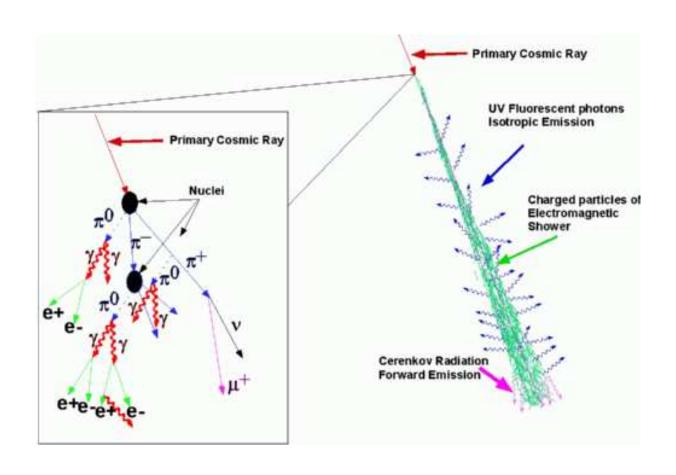
Flux: 
$$E > 10^{12} \, \mathrm{eV}$$
:  $\sim 10 \,$  primary particles / (m<sup>2</sup> min)  $E > 10^{18.5} \, \mathrm{eV}$ :  $\sim 1 \,$  primary particle / (km<sup>2</sup> year)

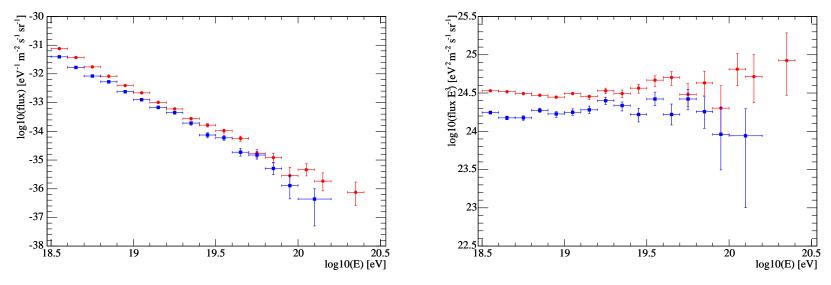
### Discrepancy between methods of detection?

- AGASA etc. detect air showers on surface of the earth secondary:  $\pi, K \cdots \to \mu \ldots$  ( $\mu$  survive  $\sim 15 \text{ km}$  to the earth). O(1) particle per GeV , up to  $10^{11}$  particles  $\to$  conclusions about energy of primary particle { shower is reconstructed with numerical methods, "max. likelihood" }
- HiRes: Fluorescence : bluish/UV light emitted from excited  $N_2$  in nights without moon light and clouds visible by telescopes.

**Heavy nuclei** as primary particles  $\rightarrow$  higher shower onset  $\rightsquigarrow$  <u>type</u> of primary particle [Record at  $3 \cdot 10^{20} \; \mathrm{eV}$  was presumably a heavy nucleus, e.g. oxygen ]

**Spallation**: heavy nuclei break apart after a while (collision in gas clouds) plus photodisintegration  $\rightarrow$  high proton fraction hints at a **long path**.

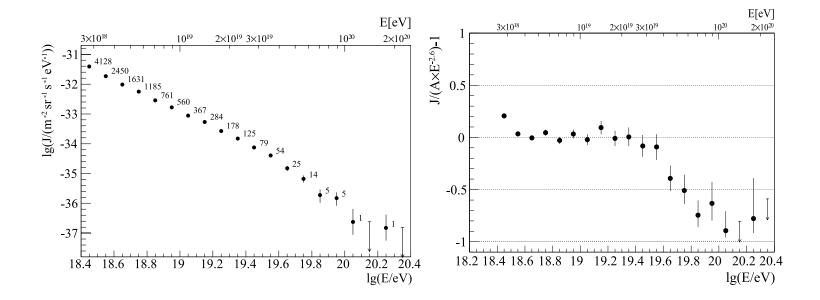




Data from AGASA vs. HiRes

Pierre Auger Project (in Argentina, operating in part since 2003, completed in 2008) combines both, hopes to resolve this issue

- on ground: water Čerenkov array 1600 water tanks over 3000 km<sup>2</sup> (sizable statistics)
- Fluorescence: 24 telescopes verify correlation and energy calibration
- ightarrow E to pprox 22% systematic error



Data by the Pierre Auger Collaboration (presented in July 2007 in Mexico)

Spectrum decays  $\propto E^{-2.69(2)}$  between  $E_{\rm ankle} \simeq 10^{18.6}~{\rm eV}$  and  $E_{\rm GZK} \simeq 10^{19.6}~{\rm eV}$ 

Clear reduction above  $E_{
m GZK}$  but some new super-GZK events...

Nov. 2007: Analysis and interpretation of arrival directions  $\rightarrow$  Appendix

Not incompatible with overall flux  $\propto E^{-3}$ , space for speculations remains E.g. violation of Lorentz symmetry (crucial for  $\sigma$  and K!) . . .

# **II. Lorentz Symmetry**

So far assumed to hold, even at  $\gamma$ -factor  $\sim 10^{11}\,$  (LEP probed up to  $\gamma \sim 10^5$ ) Central characteristic of relativity

- Special RT: holds **globally** [H.A. Lorentz (1904), H. Poincaré, A. Einstein (1905)]
- General RT : holds **locally** [ A. Einstein ( $\sim 1915$ )]

Field  $\Phi$  (scalar, 4-vector, tensor, spinor) transforms in a representation D of the Lorentz group SO(1,3),

$$\Phi(x) \to D(\Lambda)\Phi(\Lambda^{-1}x)$$
,  $\Lambda \in SO(1,3)$ .

In particular scalars remain Lorentz invariant (LI).

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<u>Theorem</u>: { LI and Locality } \Rightarrow CPT Invariance W. Pauli, G. Lüders, R. Jost (1957)
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Simultaneous charge conjugation (C), space reflection (P) and time inversion (T).

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O.W. Greenberg (2002): CPT violation \Rightarrow LI violation (LIV) (not \Leftarrow) [ CPT tests with K_0 vs. \bar{K}_0: \Delta mass (relative) < 8 \cdot 10^{-19} ]
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Direct tests of Lorentz sym. through invariance of c:

- Michelson-Morley type :  $|\Delta c/c| \lesssim 10^{-11}$
- Atomic physics : precision tests of *specific LIV parameters* e.g. spin coupling of p, n,  $e^-$  to a possible "tensor background field" : rel. deviation  $< 10^{-27}$
- Outlook: atomic clocks on ISS etc.

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Impressive, but: CPT conserving LIV \propto E^2 assume e.g. on Planck scale (M_{\rm Planck}=1/\sqrt{G}\approx 10^{28}~{\rm eV})~{\rm LIV}\sim O(1) accelerators E<10^{13}~{\rm eV}~\rightarrow~{\rm LIV}\sim O(10^{-30})
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on the other hand:

Laboratory LIV  $\sim O(10^{-25})$ , CPT violation  $\propto E ~\rightarrow~$  at  $M_{\rm Planck}~:~{\rm LIV} \sim O(10^{-10})$ 

 $\rightarrow$  CPT **even** terms are more interesting.

Cosmic rays: hope for measuring effects not far below  $M_{\rm Planck}$ ; long path! Tests for theories like string, quantum gravity etc. are conceivable. They like to install new fields in the vacuum, which may yield LIV.

Systematic Approach: (A. Kostelecký et al., since 1998)

"Standard Model Extension", Lorentz sym. breaks spontaneously. Example:

$$\mathcal{L} = i\bar{\psi}\gamma_{\mu}\partial^{\mu}\psi - g\bar{\psi}\phi\psi - ig'G_{\mu\nu}\bar{\psi}\gamma^{\mu}\partial^{\nu}\psi + \dots$$

 $\phi$  : Higgs field, SM:  $m=g\langle\phi_0
angle$ 

analogous: tensor field  $\langle G_{00} \rangle > 0$  , otherwise  $\langle G_{\mu\nu} \rangle = 0$  .

 $\Rightarrow$  modified dispersion relation for each type of particle, depending on its coupling to  $G_{\mu 
u}$ 

Kostelecký: > 100 parameters of this kind

preserve "all usual properties of the SM" (e.g.  $E, \vec{p}$ ) except for LI (and CPT).

Special RT : Goldstone boson  $\triangleq$  photon

General RT: various scenarios

Problem: why LIV at **high** energy? Tiny g': extreme hierarchy problem!

### Pragmatic Approach (S. Coleman / S. Glashow '99)

 $\mathcal{L}_{\text{eff}}$  with explicit LIV parameters of mass dim.  $\leq 4$  (renormalisable), CPT and gauge invariance persist, in addition SO(3) sym. in a "preferred frame"

• Boson field  $\vec{\Phi}$ :

$$\mathcal{L} = \dots + \frac{1}{2} \sum_{i=1}^{3} \partial_{i} \phi^{a} \varepsilon_{ab} \partial^{i} \phi^{b} \qquad (\varepsilon : \text{sym.})$$

• Dirac spinor:

$$\mathcal{L} = \cdots + i\bar{\psi}\vec{\gamma}\vec{\partial}\left[\varepsilon_{+}(1+\gamma_{5}) + \varepsilon_{-}(1-\gamma_{5})\right]\psi$$

- Pure gauge terms, e.g. for  $U(1): E^i = F^{0i}$ ,  $B^i = \frac{1}{2} \epsilon^{ijk} F_{jk}$  rot'sym., ren'able terms:  $\vec{E}^2 \vec{B}^2$ ,  $\vec{E} \cdot \vec{B}$ ,  $\vec{B}^2$ ,  $\vec{B}^2$ ,  $\vec{B}^2$ 
  - $\rightarrow$  use also in YM theories :  $\sum_a \vec{B}^a \cdot \vec{B}^a$  (a : generators)

Leads to quasi-SM with 46 LIV parameters (many from fermion generation mixing) with gauge anomaly = 0 (gauge invariance on quantum level)

Example: real scalar field with renormalised propagator

$$-iD^{-1} = (p^2 - m_0^2)f(p^2) + \varepsilon \vec{p}^2 g(p^2)$$

[ Minkowski space with c=1,  $p^2=E^2-\vec p^2$ ,  $m_0$ : renormalised at  $\varepsilon\to 0$  ] f,g: smooth functions with normalisation  $f(m_0^2)=g(m_0^2)=1$ 

LIV perturbation in  $O(\varepsilon)$  shifts the poles to

$$\begin{split} E^2 &= \vec{p}^2 + m_0^2 - \varepsilon \vec{p}^2 \simeq \vec{p}^2 c_{\rm P}^2 + m^2 c_{\rm P}^4 \\ \text{with} & m = \frac{m_0}{1+\varepsilon} \quad , \quad c_{\rm P}^2 = 1-\varepsilon \end{split}$$

Each particle receives its own Maximal Attainable Velocity (MAV).

[ Group velocity : 
$$\frac{\partial E}{\partial |\vec{p}|} = \frac{|\vec{p}|}{\sqrt{|\vec{p}|^2 + m^2 c_{\mathrm{P}}^2}} \, c_{\mathrm{P}}$$
 ]

Correction becomes significant when  $\ arepsilonec{p}^2/m_0^2 \sim O(1)$ 

 $\Rightarrow$  tiny  $\varepsilon$  could be manifest at some tremendous energy! (Hierarchy problem is back)

### Applications:

ullet Decay at ultra high energy : particle $_0 \to \sum_a$  particle $_a$  (m negligible) Decay condition:

$$|c_0|\vec{p}_0| = \sum_a c_a |\vec{p}_a| \ge c_{\min} \sum_a |\vec{p}_a| \ge c_{\min} |\vec{p}_0|$$
 $\Rightarrow c_0 \ge c_{\min} := \frac{\min}{a} c_a$ 

- Charged particle with  $c_{\rm P}/c_{\gamma}=1+\varepsilon>1$ : "Vacuum Čerenkov radiation" at  $v>c_{\gamma}$  , i.e.  $E>m/\sqrt{1-c_{\gamma}^2/c_{\rm P}^2}\simeq m/\sqrt{2\varepsilon}$
- ▶ Protons survive  $E \simeq 10^{20} \text{eV}$   $\Rightarrow$   $\varepsilon_p < \frac{m_p^2}{2E^2} \approx 5 \cdot 10^{-23}$  better than bound from atomic physics (but only upper bound)
- ▶ Cosmic e<sup>±</sup> observed up to  $E \simeq 1 \; {\rm TeV} \quad \Rightarrow \quad \varepsilon_e < 10^{-13}$

#### GZK Cutoff

Reconsider head-on collision  $p+\gamma \to \Delta(1232)$  with  $\mathbf{c}_{\gamma} = \mathbf{c}_{\Delta} = \mathbf{1}$ ,  $\mathbf{c}_{\mathbf{p}} = \mathbf{1} - \varepsilon$ 

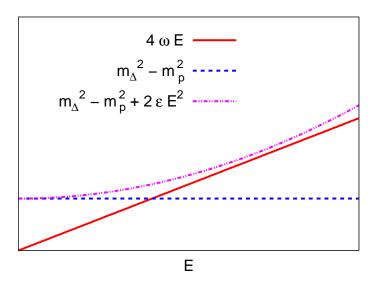
Constraint for a  $\Delta$  resonance :

$$m_{\Delta}^{2} < (E + \omega)^{2} - (p_{i} - \omega)^{2} \simeq E^{2} - p_{i}^{2} + 2\omega(E + p_{i})$$

 $E,\,p_i\,$  for a proton in the "laboratory" :

$$E^2 - p_i^2 (1 - \varepsilon)^2 = m_p^2 (1 - \varepsilon)^4 \underbrace{\longrightarrow}_{E \gg m_p, |\varepsilon| \ll 1} \underbrace{E^2 - p_i^2} \simeq m_p^2 - 2 \varepsilon E^2$$

$$\Rightarrow m_{\Delta}^2 - m_p^2 + 2 \varepsilon E^2 < 4\omega E$$
 avoids photopion production



$$m_{\Delta}^2 - m_p^2 + 2 \, \varepsilon \, E^2 < 4 \omega E$$

- lackbox At arepsilon=0 : minimal energy  $\ E_0=rac{m_\Delta^2-m_p^2}{4\omega}$
- $\blacktriangleright$  With  $\varepsilon$  included, only soluble if

$$\varepsilon < \frac{\omega}{2E_0} \simeq \frac{2\omega^2}{m_{\Delta}^2 - m_p^2} |_{\omega = 6 \cdot 10^{-4} \text{ eV}} = 1.9 \cdot 10^{-25}$$

### A tiny $\varepsilon$ could remove the GZK cutoff!

[ For slow protons the resonance  $p+\gamma \to \Delta$  persists.]

This rules out the  $\Delta$  channel for the photopion production.

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Next candidate : p+\gamma \to p^*(1435) \to p+\pi at ultra high energy : decay only for c_\pi-c_p<5\cdot 10^{-24} we could close this channel too . . .
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Farrar/Biermann (1998) : the 5 top events (  $> 10^{20}~{\rm eV}$ ) all originate from the direction of a quasar. [ Quasi-stellar radio source: extremely bright centre of a young galaxy ]

Coleman/Glashow: primary particle of the super-GZK events could be neutrons:

- $c_n < c_p$ : no  $\beta$ -decay at high energy
- $c_n < c_\Delta$  : protected from the GZK cutoff
- hardly deflected by magnetic fields

[ Today (with O(100) super-GZK events) quasar hypothesis out of fashion, but clustering of directions revitalised, neutral primary particles (?)]

# Maximal Attainable Velocities of the Neutrinos

Three bases for the neutrino states:

eigenstates of flavour, of mass  $m_0$  or of MAV  $c_{\nu}$ .

In principle neutrino oscillation is possible even at  $m_{\nu}=0$ , but not compatible with phen. data. (Lipari/Lusignoli '99)

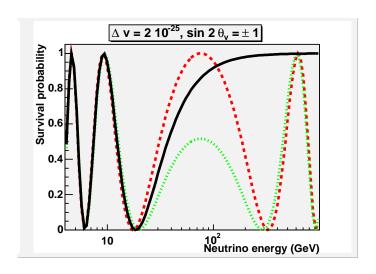
We concentrate on the oscillation  $\nu_{\mu} \leftrightarrow \nu_{\tau}$ .

Assumption: dominant effect due to flavour-mixing of the mass states, plus ev. sub-dominant effect from

$$\Delta v = \text{MAV}(\nu_1) - \text{MAV}(\nu_2)$$
  
 $\theta_v = \text{mixing angle of } |\nu_{\mu}\rangle \text{ and } |\nu_{\tau}\rangle \text{ in MAV basis .}$ 

 $\Delta v$  and  $heta_v$  modify the life time of  $\hspace{0.1cm} 
u_{\mu}$  .

Example of the MACRO Collaboration (Gran Sasso):



Survival probability of  $u_{\mu}$  over 10 000 km at  $\Delta v=2\cdot 10^{-25}$  ,  $\sin 2\theta_v=0$  , 1 , -1 .

Sensitivity at high energy of the  $\nu_{\mu}$ .

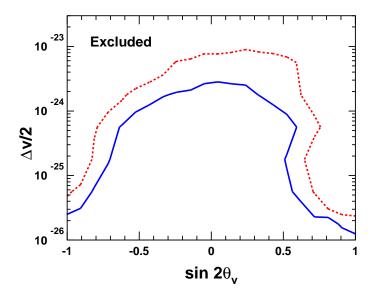
Consider a cosmic  $\nu$  with  $O(100)~{\rm GeV}$ , for  $m_{\nu} \lesssim 1~{\rm eV}$ :  $\gamma \gtrsim 10^{11}~{\rm (like~proton)}$ .

Detection of upward directed  $\,\mu\,$  from  $\,\nu_{\mu} + N 
ightarrow \mu + \dots$ 

multi-Coulomb scattering ightarrow reconstruction of  $E_{\mu}$  and  $E_{
u_{\mu}}$  ,

58 events with  $E_{\nu\mu}>130~{
m GeV}$ , compare to flux at low  $E_{\nu\mu}$ 

### Result (2004) :



Variation of  $\Delta v$  and  $\theta_v$  does not improve the fit.

For arbitrary 
$$\theta_v$$
:  $|\Delta v| < 6 \cdot 10^{-24}$  (90 % C.L.)

[ Agreement with Super-Kamiokande K2K data (Fogli et al. '99) ]

# III. Cosmic $\gamma$ -rays

We now consider the photons themselves (so far in the background).

Highest energy  $E_{\gamma} > 50~{\rm TeV}$  from Crab nebula (rest of a supernova, distance : 2 kpc).

Strongest sources beyond our galaxy :

Blazars, e.g. Markarian 501 (HEGRA, 1999),  $E_{\gamma} \approx 20 \; {\rm TeV}$ , distance 157 Mpc (from redshift).

Subset of "Active Galactic Nuclei", environment of a super-massive Black Hole, driven by swallowed matter  $\to$  emits  $\gamma, e^{\pm}\dots$ 

A few hundreds are known, here distance and direction can often be determined.

### New puzzle similar to GZK

We expect pair creation with IR background photons

$$\gamma_{\rm UV}(E) + \gamma_{\rm IR}(\omega) \rightarrow e^+ + e^- \dots [{\rm Compton\ scattering}]^{-1} \rightarrow {\rm cascade}$$

In centre-of-mass system:  $\bar{\omega}=E/\gamma=\gamma\omega$   $\to$  condition:  $\bar{\omega}^2=E\omega>m_e^2$  .

Example: for  $E\sim 10~{\rm TeV}$  scattering at  $\omega\gtrsim 3~{\rm meV}=5\langle\omega\rangle$ 

Despite the low density, this cross-section  $\sigma$  is sufficient, to practically exclude  $E_{\gamma}$  over such long distances.

Stecker/Glashow '01: Way out analogous to GZK

$$c_e = c_\gamma + \varepsilon$$

Condition for head-on collisions :  $2E\omega - \emph{E}^2 \emph{\varepsilon} > 2m_e^2$ 

 $\varepsilon > 0$  could increase the energy threshold, or avoid pair creation completely  $\Rightarrow$  Universe becomes transparent for all photons.

No pair creation for  $\varepsilon \geq \frac{2}{E^2}(E\omega-m_e^2)|_{E=20~{
m TeV},~\omega=0.003~{
m eV}}=2\cdot 10^{-15}$ 

below bound for vacuum Čerenkov radiation of the electron,  $~arepsilon < 10^{-13}$  .

However: little known radio background could resolve puzzle

# $\gamma$ -Ray-Bursts (GRB)

Emitted in powerful energy eruptions for short periods (sec. to min.), temporarily brightest  $\gamma$  source in the sky.

Sources are small, merger of Neutron Stars or Black Holes or . . .

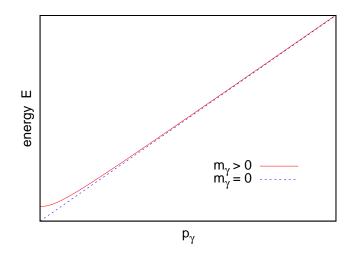
Known since 1973, homogeneous distribution,  $E_{\gamma}=10^4\dots 10^8~{\rm eV}$ 

Discovery from satellites, redshift measured from ground. Direct identification from ground more efficient (La Silla, Chile).

2005: Observation from  $4~\mathrm{Gpc}$ , i.e. from Early Universe (  $< 10^9~\mathrm{y}$  ).

Amelino-Camelia et al. : test for dispersion relation:  $v_{\gamma}(E) = \text{const.}$ ?

Simplest attempt:  $\mathbf{m}_{\gamma} > \mathbf{0}$ ,  $v_{\gamma} = \frac{\partial E}{\partial p} \neq \text{const.}$ 



Almost same time of arrival after a long journey  $\;
ightarrow\; m_{\gamma} < 2.4 \cdot 10^{-11} \; {\rm eV}$  (Schaefer, '99)

However:

much better bound from laboratory  $\,m_{\gamma} < 6 \cdot 10^{-17} \; {\rm eV}\,$  (CERN Data Booklet)

We stay with  $\, m_{\gamma} = 0 \,$  .

Here Coleman/Glashow ansatz  $E^2=p^2c_\gamma^2$  does not help.

#### "Doubly Special Relativity":

Class of theoretical approaches, which try to introduce a second absolute bound, in addition to c (Galilei: 0, Einstein: 1, are there more?)

Example: H.S. Snyder (1947): absolute minimal length (maybe Planck length  $1/M_{\rm Planck} \simeq 10^{-35} \ {\rm m}$ )

Idea: proceed as with angular momentum operator  $L_3$  from a 5d perspective (c=1).

$$S = x_0^2 - x_1^2 - x_2^2 - x_3^2 - \mathbf{x_4^2}$$

 $S=a^2$ : 4d de Sitter space inside the 5d light cone.

Generation of transformations, which leave S invariant:

$$L_{3} = \frac{\hbar}{i}(x_{1}\partial_{2} - x_{2}\partial_{1}) \quad \text{invariant} \quad x_{1}^{2} + x_{2}^{2}, x_{0}, x_{3}, x_{4}$$

$$X = \frac{a}{i}(x_{1}\partial_{4} - x_{4}\partial_{1}) \quad \dots \quad x_{1}^{2} + x_{4}^{2}, \dots \quad (4d \text{ LIV})$$

$$T = ai(x_{0}\partial_{4} + x_{4}\partial_{0}) \quad \dots \quad x_{0}^{2} - x_{4}^{2}, \dots \quad (4d \text{ LIV})$$

### Spectrum of X is discrete

$$X\psi = \lambda\psi \;, \quad \begin{pmatrix} x_1 \\ x_4 \end{pmatrix} = r \begin{pmatrix} \sin\varphi \\ \cos\varphi \end{pmatrix} \;, \quad X = \frac{a}{i}\partial_\varphi \;, \quad \psi \propto \exp(\frac{i}{a}\varphi\lambda)$$
$$\psi(\varphi) = \psi(\varphi + 2\pi) \qquad \Rightarrow \; \lambda = \frac{n}{a} \;, \quad n \in \mathbb{Z}$$

Position operators do not commute:  $[X,Y] = \frac{ia}{\hbar}L_3$  etc.

ightarrow new uncertainty relation  $\min(\Delta X \ \Delta Y) \propto a^2$ 

Minimal length a as an absolute constant, 4d non-locality, but 5d LI.

Interpretation as event horizon in a mini Black Hole matches a = Planck length (Doplicher/Fredenhagen/Roberts '95)

Currently popular version: commutators as constant "tensor field"

$$[X_{\mu}, X_{\nu}] = i\Theta_{\mu\nu}$$

observer independent, sets min. area (tensor under deformed Lorentz trafo).

Non-commutativity affects pure U(1) gauge field : picks up a YM-type self-coupling  $\,\to\,$  deformed photon dispersion

1-loop result takes the form (Matusis/Susskind/Toumbas '00)

$$E^2 = \vec{p}^2 + \frac{C}{(p\Theta)^2}$$

[ on quantum level the new UV term  $\Theta_{\mu 
u}$  causes also IR divergence (additional uncertainty !) ]

► Amelino-Camelina et al. (2003) :

Analysis of GRB radiation  $\Rightarrow \|\Theta\| > 10^{-40} \ \mathrm{cm^2}$ , otherwise effect should be *larger*. However:

- $\Theta = 0$  is <u>not</u> excluded in this way.
- C < 0 i.e. 1-loop result is actually <u>IR unstable !</u> (Landsteiner/Lopez/Tytgat '01). (SUSY cancels IR divergence . . . )

### NC QED revisited non-perturbatively (W.B./Nishimura/Susaki/Volkholz '06)

- ullet Commutative plane  $(x_3,x_4) \rightarrow {\sf Lattice}$  includes Euclidean time (enables transition to Minkowski signature)
- ullet NC plane  $(\hat{x}_1,\hat{x}_2)$ ,  $[\hat{x}_1,\hat{x}_2]=i heta$  Lattice structure :  $\exp\left(irac{2\pi}{a}\hat{x}_{\mu}
  ight)=\hat{1}$   $(\mu=1,2)$

Momenta commute, usual periodicity

$$e^{ik\mu\hat{x}\mu} = e^{i(k\mu + \frac{2\pi}{a})\hat{x}\mu}$$

$$\hat{1} = e^{i(k\mu + \frac{2\pi}{a})\hat{x}\mu} e^{-ik\nu\hat{x}\nu} = \dots = \hat{1} \exp\left(\frac{i\pi}{a}\theta(k_2 - k_1)\right)$$

$$\Rightarrow \frac{\theta}{2a}k_\mu \in \mathbb{Z} : \text{momenta discrete, lattice periodic}$$

Periodic  $N \times N$  lattice:  $k_{\mu} = \frac{2\pi}{aN} n_{\mu} \quad (n_{\mu} \in \mathbb{Z}) \quad \Rightarrow \quad \underline{\theta = \frac{1}{\pi} \mathbf{N} \mathbf{a}^2}$ 

<u>Double Scaling Limit</u>: continuum  $a \to 0$  infinite volume  $Na \to \infty$   $Na^2 = \text{const.}$ 

Simultaneous UV and IR limit, which keeps  $\theta = \mathrm{const.}$  (Szabo '01)

U(1) gauge theory on a NC lattice can be mapped onto a "twisted Eguchi-Kawai model" (U(N) matrices in one point) (Ambjørn et al. '01)  $\to$  numerically tractable

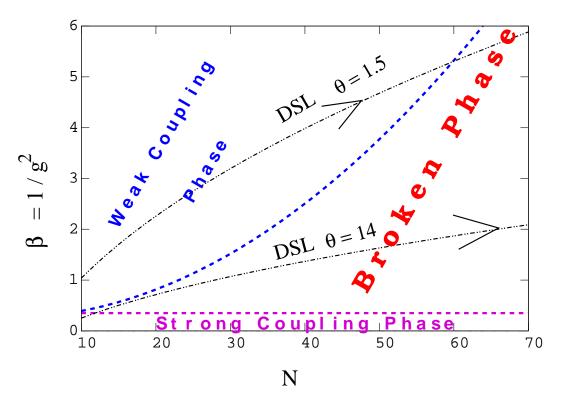
Yang-Mills type self-interaction and gauge transformations are **non-local** on scale  $\sqrt{|\theta|}$ .

In this range: gauge invariant open Wilson lines carry momentum  $\rightarrow$  order parameters for spont. breaking of transl. sym.

Numerical observation:

Double Scaling Limit  $\beta \equiv \frac{1}{g^2} \propto \sqrt{N}$  stabilises a variety of observables  $(a=1/\beta)$ 

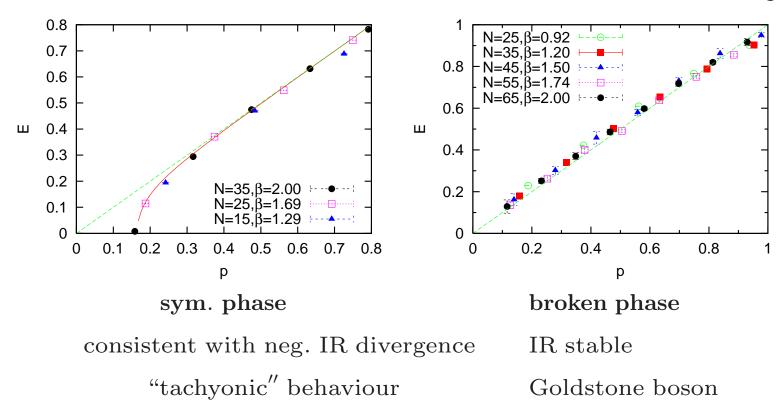
Phase diagram : weak  $\leftrightarrow$  moderate  $\leftrightarrow$  strong coupling



Double Scaling Limit  $\, eta \propto \sqrt{N} \,$  always leads to the phase of broken symmetry.

That phase could describe a stable cont. limit for the NC photon.

Dispersion relation: determined from exp. decay in comm. plane  $E(p=p_3)|_{p_1=p_2=0}$ 



### Photon may survive in an NC world,

but explicit prediction for the deformed dispersion relation is outstanding.

• Return to a pragmatic ansatz: J. Ellis et al. (2006/7)

$$c^{2}|\vec{p}|^{2} = E^{2}\left(1 + \frac{E}{M}\right)$$
  
 $\rightarrow v_{\gamma}(E) = \frac{\partial E}{\partial |\vec{p}|} \simeq c\left(1 - \frac{E}{M}\right)$ 

M: very heavy mass, emerges somehow from "quantum gravity foam", noticeable at high energy, or after a long path.

### Analysis of 35 GRB's

Data from 3 satellites [e.g. HETE:  $dt=64~\mathrm{ms}$ , 4 energy channels].

High energy  $\gamma$ 's arrive later. Ansatz for the observed delay without LIV

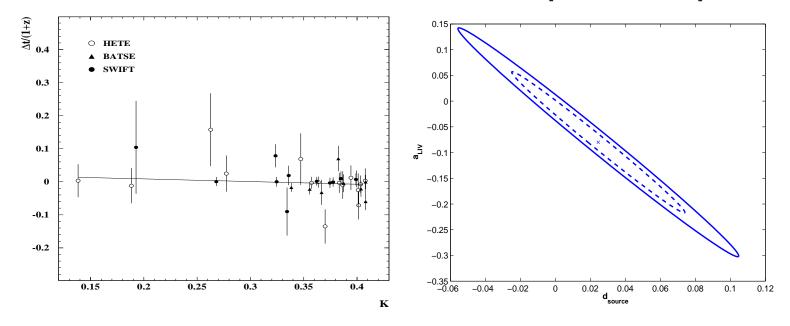
$$\Delta t_{\rm obs} = d_{\rm source}(1+z)$$

 $d_{
m source}$  : possible delay already in the emission

z: redshift

With LIV: 
$$\frac{\Delta t_{\rm obs}}{1+z} = d_{\rm source} + \underbrace{\frac{\Delta E}{M} \frac{1}{H_0}}_{a_{\rm LIV}} K(z)$$
 (K : complicated correction)

Enhance error bars until fits match: 1  $\sigma$  evidence for LIV [ 68 %, 95 % ]



Cautious conclusion :  $|\mathbf{M}| > 1.4 \cdot 10^{25} \ \mathrm{eV} \approx 0.001 \ M_{\mathrm{Planck}}$  (with 95 % C.L.)

Studies of single GRBs or blazar flares (e.g. Mkn501, Mkn 421) even conclude  $|M| > 0.01 M_{\rm Planck}$ 

# **Conclusions:**

Cosmic rays: unique opportunity for phenomenological access to tremendous energies.

In the centre-of-mass frame, relevant processes are harmless low energy events → Question of LI is crucial!

### GZK and $\gamma$ -TeV Puzzle :

Why is the Universe surprisingly transparent for

• protons with  $E_p \gtrsim 10^{20} \; \mathrm{eV}$  • photons with  $E_\gamma \gtrsim 10 \; \mathrm{TeV}$  ?

Open question; LIV provides a class of proposals for a solution, IF some puzzle persists

LIV not detected anywhere — we discussed failed attempts with cosmic neutrinos and GRBs. But established LI precision does not exclude proposed solutions.

New projects include: Japanese Experiment Module – Extreme Universe Space Observatory (JEM-EUSO), Orbiting Wide-angle Light-collectors (OWL): search for fluorescence light from satellites. Pierre Auger: new plant in northern hemisphere . . .

# News in Nov. 2007: AGN Hypothesis

[Active Galactic Nuclei: in centre a super-massive black hole (  $> 10^6$  solar masses), nucleus attracts and absorbs large quantities of matter, but emits high-E particles (mechanism?)]

Pierre Auger Collab. analyses UHECRs detected from Jan. 2004 - May 2006

### Hypothesis: directions are clustered and correlated with locations of nearby AGN

3 parameters:  $\psi$  : angular range around UHECR direction

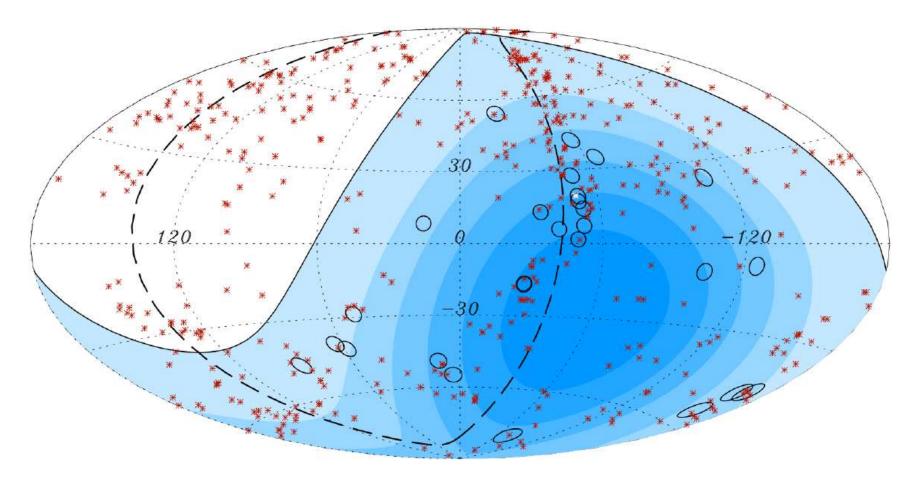
 $E_{
m min}$  : threshold for UHECR

 $R_{
m max}$ : max. distance to "nearby" AGN (from redshift)

```
tuning \rightarrow (\psi, E_{\rm min}, R_{\rm max}) = (3.1^{\circ}, 5.6 \cdot 10^{19} \ {\rm eV}, 75 \ {\rm Mpc}) yields max. correlation, captures 12 our of 15 UHECR (for isotropic sources: 3.2 expected [at fixed parameters . . . ])
```

 $R_{\rm max}$  short,  $\approx$  straight UHECR propagation conceivable

Check with data from May 2006 - Aug. 2007: captures 8 out of 13 UHECRs (2.8 expected)



Celestial sphere with circles of radius  $3.1^\circ$  at arrival directions of 27 UHECRs detected by the Pierre Auger Observatory. Asterisks: 472 AGN with R < 75 Mpc.

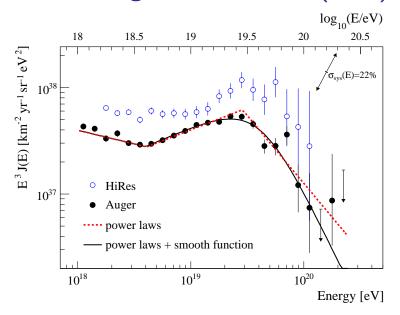
Dashed: supergalactic plane; white: Centaurus A

For clustering PA Collab. claims 99 % C.L., correlation less clear

#### **Critics:**

- Variation of  $(\psi, E_{\min}, R_{\max})$  is discussed only vaguely.
- Statistics still small, world data before essentially isotropic [AGASA (1996): slight signal for clustering, contradicted by HiRes] Consistent with world data?
- Gorbunov/Tinyakov/Tkachev/Troisky: Flux  $\propto 1/R^2 \rightarrow \text{nearest}$  AGN should be dominant sources in particular Cen A and Virgo should contribute each  $\approx 6$  events out of 27 Cen A in business, but Virgo delivers none  $\Rightarrow$  AGN Hypothesis <u>disfavoured</u> at 99 % C.L. [However: argument could be evaded if AGN are *episodic* UHECR sources]
- D. Fargion: short  $R_{\text{max}}$  favours heavy nuclei as primaries
- Hypothesis supported by new Irkutsk data analysis, but not by HiRes.

### **Updated spectrum: Pierre Auger Collaboration (2010)**



flux (
$$E \lesssim E_{\rm ankle} \simeq 10^{18.6}~{\rm eV}) \propto E^{-3.3}$$
 (stat. errors with Feldman/Cousins method)

flux 
$$(E_{\rm ankle} < E < E_{\rm GZK} \simeq 10^{19.6} \; {\rm eV}) \propto E^{-2.6}$$

Just beyond : clearly suppressed,  $\mathit{but}$  in good agreement with  $E^{-3.3}$  extrapolation

**GZK** cutoff is substantiated (?)

### **Clustering and AGN Hypotheses**

period	exposure	events	AGN	isotropically
	$[km^2 sr yr]$	above $E_{\min}$	direction	expected
until May 2006	4390	14	9	2.9
June 2006 - Aug. 2007	4500	13	9	2.7
Sept. 2007 - March 2009	8150	31	8	6.5

1. period: exploratory, used to fix paramters ( $\rightarrow$  biased)

 $E_{\rm min}$  shifted down to  $5.5 \cdot 10^{19}~{\rm eV}$  (calibration corrected)

Critics addressed: Virgo passivity persisits, but only 1.2 events expected "masked data" excluding vicinity of galactic plane  $(12^{\circ})$ : no drastic change

New data with exposure almost doubled: "neither strenghten nor contradict" hypotheses of clustering and ANG correlation. Overall still supported (in particular clustering), but evidence became clearly weaker.

Probability for accidental isotropic effect: p = 0.0004 (2006/7), p = 0.33 (2007/9).